Arnaud Goussebaile

Actinfo Chair, Institut Louis Bachelier, CREST

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#### Motivation



Figure: New York hit by Hurricane Sandy in October 2012 (Source: WNYC)

Introduction

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- ▶ How do cities spatially develop in terms of **density** and **resilience** at each location?
- ▶ What is the impact of **insurance subsidization or public relief** on city development?
- ▶ What **urban policies** should we implement in terms of density and resilience?
- ▶ How **urban growth and climate change** affect city development?

#### Results

Introduction

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#### City development:

- Riskier areas are developed nearer to the city center than further away.
- ► At a given distance to the city center, riskier areas are usually associated with lower housing density and higher building resilience.

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- Actuarially fair insurance implements optimal housing density and building resilience.
- Insurance subsidization usually leads to housing over-development and resilience under-investment in risky areas.

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Model

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- Insurance subsidization usually leads to housing over-development and resilience under-investment in risky areas.

#### Long-term evolution:

- Urban growth leads to housing density increase and building resilience increase.
- Climate change usually leads to density decrease and resilience increase.



#### Literature review

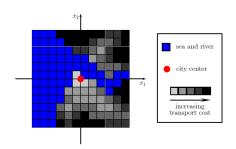
Introduction

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- theoretical:
  - natural disasters and urban density: Polinsky and Shavell (1976); Scawthorn et al. (1982); Frame (1998,2001): Grislain-Letremy and Villeneuve (2014);
  - natural disasters, urban density and resilience investment: the present paper
- empirical:
  - natural disasters and housing prices: Shilling et al. (1989); McKenzie and Levendis (2008); Daniel et al. (2009); Atreya and Czajkowski (2014);
  - natural disasters and resilience investment: Kunreuther et al. (1978); Burby et al. (1988); Czajkowski and Simmons (2013); Aerts, Michel-Kerjan et al. (2014).



Static spatial model with coordinates  $x = (x_1, x_2)$ .



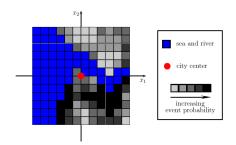


Figure: Commuting transport costs  $t(x)=t(x_1,x_2)$ 

Figure: Natural disaster probabilities 
$$\pi_{\mu}(x) = \pi_{\mu}(x_1, x_2)$$

Results

# Housing developers and land markets

- ▶ Identical housing developers in competition:
  - ▶ they acquire land at unit price  $p_l(x)$ ,
  - ▶ they develop housing services H(x) per land unit with building resilience B(x) per land unit at cost C(H(x), B(x)),
  - they sell housing at unit price  $p_h(x)$ .



Model

- ▶ Identical housing developers in competition:
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  - ▶ they develop housing services H(x) per land unit with building resilience B(x) per land unit at cost C(H(x), B(x)),
  - they sell housing at unit price  $p_h(x)$ .
- Because of competition, the land unit price is such that:

$$p_{l}(x) = \max_{H(x),B(x)} \left( p_{h}(x)H(x) - C(H(x),B(x)) \right)$$
s.t.  $H(x) \ge 0$ ,  $B(x) \ge 0$  and (2).



# Households and housing markets

- N identical households in competition with utility function v(z,h)and wealth  $\overline{y}$ :
  - they choose location x, composite good consumption z(x) at unit price 1 and housing services h(x) at unit price  $p_h(x)$ ,
  - they incur commuting transports cost t(x) and natural disaster costs  $(1-\lambda)\pi_{\mu}(x)\frac{h(x)}{H(x)}L(H(x),B(x))+\overline{\tau}$ .

# Households and housing markets

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  - they incur commuting transports cost t(x) and natural disaster costs  $(1-\lambda)\pi_{\mu}(x)\frac{h(x)}{H(x)}L(H(x),B(x))+\overline{\tau}$ .
- Because of competition, the housing unit price is such that:

$$p_h(x) = \max_{z(x),h(x)} \frac{\overline{y} - z(x) - t(x) - (1 - \lambda)\pi_{\mu}(x)\frac{h(x)}{H(x)}L(H(x),B(x)) - \overline{\tau}}{h(x)}$$

s.t. 
$$v(z(x), h(x)) = \overline{v}$$
.

(2)



# Closing the model

The city boundaries correspond to locations x such that  $p_l(x) = \overline{p_a}$ . The boundaries can also be characterized by an upper natural disaster probability  $\pi_{\mu}^*(t)$  over which land is not developed.

# Closing the model

- ▶ The city boundaries correspond to locations x such that  $p_l(x) = \overline{p_a}$ . The boundaries can also be characterized by an upper natural disaster probability  $\pi_u^*(t)$  over which land is not developed.
- $\triangleright$  With n(x) the household density at location x, the clearing housing market condition and the population condition can be written:

$$n(x)h(x)=H(x),$$

$$N = \iint n(x) dx_1 dx_2.$$



# Developed areas and city boundaries

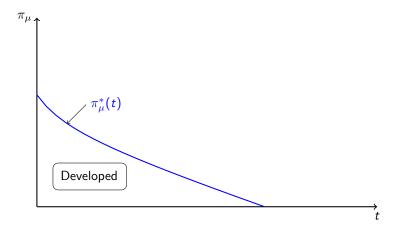


Figure: Developed areas (as a function of transport cost t and disaster risk  $\pi_{\mu}$ )



# Developed areas and city boundaries

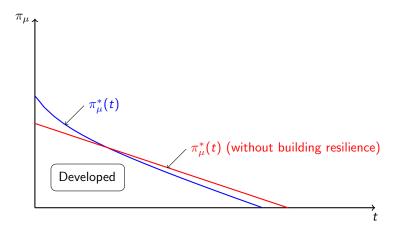


Figure: Developed areas (as a function of transport cost t and disaster risk  $\pi_u$ )



# Developed areas near New York city center



Figure: Extension of New York city center over water areas thanks to land fill (Source: www.nyc.gov/)

### Housing services and building resilience

▶ The housing density H(x) and building resilience B(x) vary in space as follows:

$$\frac{dH}{d\overset{\rightarrow}{x}} = \underbrace{-\frac{1}{h(x)A_1(x)}}_{<0} \underbrace{\frac{dt}{d\overset{\rightarrow}{x}}} + \left(\underbrace{-\frac{(1-\lambda)}{A_1(x)}\frac{\partial L}{\partial H}}_{<0 \text{ (direct)}} + \underbrace{\frac{(1-\lambda)A_2(x)}{A_1(x)}\frac{\partial L}{\partial B}}_{>0 \text{ (indirect)}}\right) \frac{d\pi_{\mu}}{d\overset{\rightarrow}{x}},$$

$$\frac{dB}{d\overrightarrow{x}} = \underbrace{\frac{A_4(x)}{h(x)A_3(x)}}_{<0} \underbrace{\frac{dt}{d\overrightarrow{x}}} + \left(\underbrace{-\frac{(1-\lambda)}{A_3(x)}\frac{\partial L}{\partial B}}_{>0 \text{ (direct)}} + \underbrace{\frac{(1-\lambda)A_4(x)}{A_3(x)}\frac{\partial L}{\partial H}}_{<0 \text{ (indirect)}}\right) \frac{d\pi_{\mu}}{d\overrightarrow{x}},$$

# Actuarially fair insurance

Actuarially fair insurance ( $\lambda=0$ ) leads to a Pareto-optimal allocation.



# Insurance subsidies and developed areas

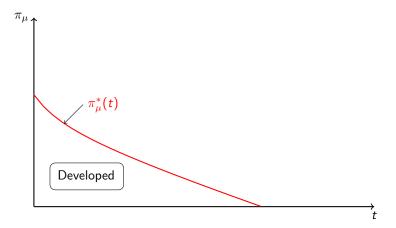


Figure: Developed areas with country subsidies

### Insurance subsidies and developed areas

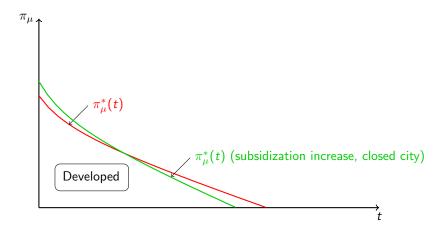


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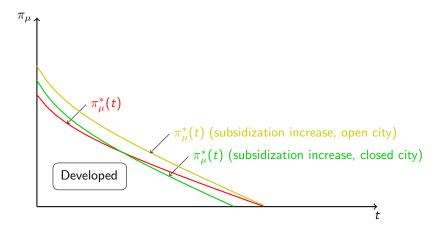


Figure: Developed areas with country subsidies

### Insurance subsidies, housing and resilience

▶ The increase of insurance subsidization has the following impact on urban development at each location x in the city:

$$\frac{dH(x)}{d\lambda} = \underbrace{\frac{\pi_{\mu}(x)}{A_{1}(x)}\frac{\partial L}{\partial H}}_{>0 \ (\textit{direct})} - \underbrace{\frac{\pi_{\mu}(x)A_{2}(x)}{A_{1}(x)}\frac{\partial L}{\partial B}}_{>0 \ (\textit{indirect})} - \underbrace{\frac{1}{h(x)A_{1}(x)}\frac{d\overline{\tau}}{d\lambda}}_{\geq 0},$$

$$\frac{dB(x)}{d\lambda} = \underbrace{\frac{\pi_{\mu}(x)}{A_3(x)} \frac{\partial L}{\partial B}}_{<0 \ (direct)} - \underbrace{\frac{\pi_{\mu}(x)A_4(x)}{A_3(x)} \frac{\partial L}{\partial H}}_{<0 \ (indirect)} + \underbrace{\frac{A_4(x)}{h(x)A_3(x)} \frac{d\overline{\tau}}{d\lambda}}_{\leq 0},$$

### Urban growth

▶ With an open city, a wealth increase affects housing and resilience at each location x as follows:

$$\frac{dH(x)}{d\overline{y}} = \frac{1}{h(x)A_1(x)} > 0,$$

$$\frac{dB(x)}{d\overline{y}} = -\frac{A_4(x)}{h(x)A_3(x)} > 0.$$

# Climate change

With an open city, a risk increase affects housing and resilience at each location x as follows:

$$\frac{dH(x)}{d\mu} = \left(\underbrace{-\frac{(1-\lambda)}{A_1(x)}\frac{\partial L}{\partial H}}_{<0 \ (\textit{direct})} + \underbrace{\frac{(1-\lambda)A_2(x)}{A_1(x)}\frac{\partial L}{\partial B}}_{>0 \ (\textit{indirect})}\right) \frac{d\pi_{\mu}(x)}{d\mu},$$

$$\frac{dB(x)}{d\mu} = \left(\underbrace{-\frac{(1-\lambda)}{A_3(x)}\frac{\partial L}{\partial B}}_{>0 \ (direct)} + \underbrace{\frac{(1-\lambda)A_4(x)}{A_3(x)}\frac{\partial L}{\partial H}}_{<0 \ (indirect)}\right) \frac{d\pi_{\mu}(x)}{d\mu},$$

#### Conclusion

- Role of resilience investment:
  - Resilience investment allows to reallocate households from the outer boundary to risky areas near the city center.

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#### Policy recommendations:

- Actuarially fair insurance should be implemented to obtain optimal density and resilience.
- In case of insurance subsidization, density restrictions and building codes can be enforced to limit risk over-exposure.



#### Conclusion

#### Role of resilience investment:

Resilience investment allows to reallocate households from the outer boundary to risky areas near the city center.

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- Actuarially fair insurance should be implemented to obtain optimal density and resilience.
- ▶ In case of insurance subsidization, density restrictions and building codes can be enforced to limit risk over-exposure.

#### ► Further works:

- Application and welfare analysis for a city such as New York.
- Extension to household heterogeneity for inequality issues.

